X-ray study of the ferroelectric \([\text{Ba}_{0.6}\text{Sr}_{0.4}][(\text{YTa})_{0.03}\text{Ti}_{0.94}]\text{O}_3\)

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We have studied the system \([\text{Ba}_{0.6}\text{Sr}_{0.4}][(\text{YTa})_{0.03}\text{Ti}_{0.94}]\text{O}_3\), as produced using two different sintering temperatures. It was shown by others that for a sample sintered at 1550 °C the material is a relaxor, whereas for the same composition produced with sintering temperature of 1600 °C the sample is a normal ferroelectric. We have employed analysis of x-ray diffraction peak broadening, Ti K edge x ray near edge spectroscopy, and extended x-ray absorption fine structure spectroscopy of Ta and Y sites in our study. We find that the 1550 °C sinter sample has over double the lattice strain as does the 1600 °C sample. For the lower temperature sinter material, both Ta and Y go to sites substitutional for Ti in the lattice, with a significant expansion (contraction) of the local perovskite structure about Y (Ta) dopants. Thus, with only three percent B site addition of Y and Ta dopants, there is a strain associated relaxor behavior produced in a bulk sample. For the higher temperature sinter specimen, there is a marked change in the average Y environment relative to the lower temperature sinter sample.

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I. INTRODUCTION

Potrepka et al. have shown that charge-balanced substitutions of \(\text{Y}^{3+}\) and \(\text{Ta}^{5+}\) ions into \(\text{Ba}_x\text{Sr}_{1-x}\text{TiO}_3\) (BST) can lead to a broadening of the temperature dependence of ferroelectric properties. Such relaxorlike behavior can be desirable in applications that emphasize device tunability, such as, in capacitors of dynamical random access memory, infrared pyroelectric sensors, electro-optics, and tunable microwave devices.

Besides high capacitance and low losses, a lessening of temperature dependence of the dielectric properties is required for many applications. Potrepka et al. have discovered a marked effect of changes in \([\text{Ba}_{0.6}\text{Sr}_{0.4}][(\text{YTa})_{0.03}\text{Ti}_{0.94}]\text{O}_3\), as sintered at 1550 °C (sample A) versus 1600 °C (sample B). In these materials, it is presumed by Potrepka et al. that Ta substitutes for \(\text{Ti}^{4+}\) as a \(\text{Ta}^{5+}\) ion and Y substitutes for \(\text{Ti}^{4+}\) as a \(\text{Y}^{3+}\) ion. A plot of real relative permittivity versus temperature shows a sharp peak at −60 °C for sample B. Such a peak is absent for A. Even at room temperature, for which our composition of BST is paraelectric, the relative permeability of B significantly exceeds that of A by about 50%. One way of summarizing these results would be to state that sample A is much more “relaxor” like than B if we mean by relaxor behavior that there is a “diffuseness of the temperature dependence of the various properties that relate to the polarization of the material.”

An illustration of a perovskite unit cell with a much exaggerated tetragonal distortion is shown in Fig. 1. At room temperature, BST is found, by x-ray diffraction (XRD), to be cubic for \(x < 0.7\). Our samples have a value of \(x\) of 0.6 and are therefore expected to appear cubic, as verified by our XRD characterization. Despite the fact that our experiments were carried out at room temperature on paraelectric samples, we find, in agreement with other investigators, that the Ti atom location, measured locally, is not at the center of the surrounding oxygen octahedron, but displaced from the center. It is now well established for a number of perovskite ferroelectrics that local Ti displacements persist in the paraelectric phase, despite the fact that the spatially averaged structure observed by XRD is cubic. Furthermore, there is evidence that for particle sizes less than 0.1 μm, the tetragonal distortion and ferroelectricity in cubic \(\text{BaTiO}_3\) may be suppressed, even for temperatures much less than the \(T_C\) of bulk material.

![Image](365x110 to 509x301)

FIG. 1. Schematic illustration of perovskite structure in tetragonal phase of ferroelectric BST as inferred from x-ray diffraction. Under our conditions the average structure observed by x-ray diffraction is cubic.
BaTiO₃ at room temperature, the tetragonal distortion is found by XRD to be quite small, with a $c/a$ ratio of only 1.01. Crowne et al. have modeled this Ta/Y doped BST system in terms of internal electric fields associated with nonrandom clustering of the Y$^{3+}$ and Ta$^{5+}$ ions. In this model, charge compensation occurs at the Ti$^{4+}$ sites where substitutional occupancy of Ta$^{5+}$ or Y$^{3+}$ is localized, so that clustering Ta$^{5+}$ and Y$^{3+}$ impurities form permanent dipoles.

Characteristic relaxor behavior is manifested as a broadening of the temperature dependence of various polarization-dependent properties. Two early models proposed to describe relaxor behavior are the composition fluctuation model of Smolenskii et al. and the domain size effect model of Cross. Smolenskii suggested that compositional fluctuations, on the nanoscale, lead to fluctuations in ferroelectric Curie temperature in disordered material. In the model of Cross, one can have a situation in which the domain size is sufficiently small that the polarization direction is altered by thermal agitation. The temperature at which the polarization direction can be switched back and forth by thermal energies depends on the size of the domain. Consequently, in a sample with many small domains, but of different domain sizes, there will be a suite of differing Curie temperatures, and consequently, relaxor behavior. Cross points out the analogy between this type of domain size determined ferroelectric Curie temperature and the “blocking temperature” effect observed in nanoscale ferromagnets.

Subsequent to the Smolenskii and Cross models, there have been other explanations proposed for relaxor behavior. Viehland et al. suggest that relaxor ferroelectrics are analogous to magnetic spin glass systems, and will exhibit thermally activated polarization fluctuations above a freezing temperature. Westphal et al. propose that relaxor behavior originates from quenched random electric fields, a model that is along the lines of the treatment of $[\text{Ba}_{0.9}\text{Sr}_{0.1}] [\text{Y}\text{Ta}_{0.05}\text{Ti}_{0.95}]\text{O}_3$ by Crowne et al. mentioned above. For the present study, it is important to consider the possible effects of internal strains. A linear augmented plane wave method, charge compensation occurs at the Ti$^{4+}$ sites where substitutional occupancy of Ta$^{5+}$ or Y$^{3+}$ is localized, so that clustering Ta$^{5+}$ and Y$^{3+}$ impurities form permanent dipoles.

In the present study, we have investigated the Ta, Y doped BST system by XRD peak broadening analysis, Ti K-edge x-ray absorption near edge spectroscopy (XANES), and Ta L₃ and Y K-edge extended x-ray absorption edge fine structure (EXAFS).

II. EXPERIMENTAL DETAILS

The preparation of the $[\text{Ba}_{0.9}\text{Sr}_{0.1}] [\text{Y}\text{Ta}_{0.05}\text{Ti}_{0.95}]\text{O}_3$ material is described by Potrepka et al. Starting materials of 99.9% purity or better were mixed until homogeneous, then compacted with a steel die and calcined in air at 1100 °C for 8 h. The calcined materials were then reground to powders with 75 μm or smaller grain size, pressed at 50 kpsi in an isostatic press, and sintered at the respective sinter temperature in air for 40 h. The samples were bulk ceramics during the measurements, not single crystalline. We also include samples of pure SrTiO₃, and undoped Ba₁₀.₆Sr₀.₄(TiO₂₃) (BST) as part of our study. Existing data on BaTiO₃ and EuTiO₃ are used for reference. X-ray diffraction characterization is performed on all samples studied. The SrTiO₃, BST, and both Ta/Y doped BST samples are found to be pure cubic phase material. The diffraction peak intensities indicate no significant preferred orientation. No oxide diffraction peaks were found for either sample. We note that the ratio of Ba to Sr in our BST is just smaller than the critical concentration for the cubic to tetragonal transition at room temperature.

The XAFS studies of Ti edges were performed at the X-11B beam line at the National Synchrotron Light Source (NSLS). The Si (111) reflection was used for the beam line monochromator. The Ti K-edge XANES were obtained in the fluorescence mode, using an ion chamber. A common problem in obtaining XAFS data for crystalline samples is due to the fact that as the incident beam energy is increased, the Ewald sphere radius increases and the sphere suddenly will intersect reciprocal lattice points during the scan. This diffraction peak problem can often be solved by sample spinning, which is a standard technique in such cases. The BST, SrTiO₃, and both Ta, Y doped BST samples were spun. As will be seen below, the Ti K-edge x-ray absorption near edge spectra (XANES) were nearly identical for the BST as for the Ta and Y doped BST corresponding to samples A and B. In addition, some data was collected for Ti edges of samples A and B without sample spinning and identical XANES was obtained as with spinning, showing that diffraction peak effects on the XAFS were not present.

For the diffraction peak width analysis, a Bragg-Brentano diffractometer was used, outfitted with a copper anode and graphite monochromator. Reference data were taken using a LaB₆ standard purchased from NIST. The Ta L₃ edges of samples A and B were obtained at the X-11B line of the NSLS, using three scans for each sample, a Si(111) monochromator, and an ion chamber with argon counter gas. The Y K-edges presented a special problem, in that Y is just to the right of Sr in the periodic table. Therefore, the dilute Y K-edge lies on top of the intense background of the Sr absorption edge. Fortunately, however, the Sr and Y edges are sufficiently separated in energy that the Sr EXAFS oscillations do not interfere with the Y signal. Under these circumstances, a method developed by Heald can be used, and data was obtained, using this method, at the sector 20 PNC/XOR bending magnet beam line of the Advanced Photon Source (APS). In Heald’s method, one uses a multielement energy dispersive detector. The saturation effects in the energy dispersive detector, due to the rejected Sr background, are corrected for using the following procedure: The Sr and Y fluorescence energies are separately windowed, and the fluorescence Y XAFS is normalized, not with the incident photon ion chamber signal, but with the Sr signal. Both windowed energies, for dilute Y on top of a concentrated Sr background, have the same “pile up” distortion and the distortion is therefore corrected for by normalizing with the Sr signal.
FIG. 2. XRD data obtained on samples A and B, with the Kα₂
line stripped from the data. Diffraction scans shown are in the re-
region of the (220) reflection, using a copper anode diffractometer.
The peaks are normalized to exhibit the same maximum value, for
ease in visualization. Thus, the count rate shown on the ordinate
scale refers to sample B. The broader peak of sample A is normal-
ized to peak B.

III. EXPERIMENTAL RESULTS

A. Diffraction peak broadening analysis

We have analyzed the full width at half maximum (FWHM) of the diffusion peaks of samples A and B. The Kα₂ component of the peaks was stripped from the data by appropriate software, and slow scans taken over all peaks well into the wings. The diffraction patterns are fit well assuming cubic material, which simplifies the analysis. A comparison of diffraction peaks for the typical (220) reflection, samples A and B, is shown in Fig. 2. This figure illustrates that for the high angle reflections, which are particularly sensitive to lattice strains, the width of the peaks for our sample A significantly exceeds the width for sample B. The data are analyzed systematically using the Williamson-Hall relationship\textsuperscript{17,18} given by the expression below

\[ \Gamma \cos \theta = \frac{\lambda}{L} + 2 \left( \frac{\Delta d}{d} \right) \sin \theta, \]

where \( \Gamma \) is the FWHM of twice the Bragg angle, \( L \) is the
particle size, and the other symbols have the usual meaning for x-ray diffraction. By plotting \( \Gamma \cos \theta \) versus \( \sin \theta \), one obtains a linear relationship. The intercept may be used to determine the particle size and the slope determines the
strain term \( \Delta d/d \).

One must, however, account for the instrumental broadening of the diffractometer in such studies. One method which has been used is to use a LaB₆ standard material to calibrate the instrument. This material is thoroughly characterized by NIST and has negligible strain broadening. For some applications, the peak broadening due to particle size effects has been assumed to be negligible for LaB₆. However, in our application we found that the particle size broadening of the LaB₆ diffraction peaks could not be neglected relative to the broadening of the diffraction peaks of samples A and B. The sizes of the crystallites in LaB₆ range from 2 to 5 μm,\textsuperscript{19} as measured by NIST using a scanning electron microscope (SEM). By comparison, Potrepka \textit{et al.} have made SEM estimates of sample grain sizes corresponding to BST with differing concentrations of equal Ta and Y dopants.\textsuperscript{2} In the case corresponding to our samples A and B, the average grain size for the 1600 °C sinter was approximately 2 μm and the grain size of the 1550 °C sinter roughly half this value.\textsuperscript{2} These grain sizes are sufficiently large, and the consequent broadening sufficiently small, that the broadening introduced by both the diffractometer (instrumental) and the LaB₆ (inherent broadening due to particle size) in a LaB₆ XRD scan can each be an appreciable fraction of the total peak broadening of samples A and B. In our case merely subtracting LaB₆ peak widths from experimental widths could result in an overcorrection for the instrumental broadening effect. However, something can be learned from the slope of a plot, if not the intercept, of the difference between the widths of the samples and the LaB₆ standard, since the strain broadening of LaB₆ is negligible. Using slope values of the linear fits from such a graph, the strain term \( \Delta d/d \) was determined separately for samples A and B. These strains are 5.1 \( \times 10^{-3} \) and 2.2 \( \times 10^{-3} \), respectively.

We further devised a modified version of the Williamson-Hall plot appropriate to this situation. Let \( \Gamma_A \) be the FWHM of a peak corresponding to sample A and \( \Gamma_B \) be the corresponding width for sample B. \( L_A \) and \( L_B \) are the particle size of samples A and B, respectively. For any particular angle the instrumental contribution will be the same for both \( \Gamma_A \) and \( \Gamma_B \) and therefore one can plot the relationship shown below

\[ (\Gamma_A - \Gamma_B) \cos \theta = \lambda \left( \frac{1}{L_A} - \frac{1}{L_B} \right) + 2 \left( \frac{\Delta d}{d} \right)_A, \]

\[ (\Gamma_B - \Gamma_B) \cos \theta = \lambda \left( \frac{1}{L_A} - \frac{1}{L_B} \right) + 2 \left( \frac{\Delta d}{d} \right)_B. \]

Relationship (2) above has the advantage that the instrumental contribution to the broadening is subtracted from the equation. One obtains the \textit{difference} between the microstrain terms of the 1550 °C and 1600 °C sintered samples directly from the slope of a plot of \( (\Gamma_A - \Gamma_B) \cos \theta \) versus \( \sin \theta \). One can also test the grain sizes obtained, for consistency with the previously measured SEM results. Figure 3 shows a plot of Eq. (2), fit to a straight line by linear regression. From the intercept, and taking into account the standard error, we obtain the result given below

\[ \left( \frac{1}{L_A} - \frac{1}{L_B} \right) = 1.9 \pm 1.3 \text{ (μm)}^{-1}. \]

If we assume, from the SEM study of Potrepka \textit{et al.},\textsuperscript{2} that \( L_B \) is roughly 2.0 μm, then the limits in Eq. (3) yield a value of \( L_A \) between 0.26 μm and 0.87 μm. These values are somewhat smaller than, but within a factor \( \sim 3 \), consistent with the values obtained by SEM for the 1550 °C sinter sample. The difference in strain between samples can be extracted directly from the slope of this curve and agrees with the difference between the strains of A and B given in the previous paragraph.
XANES are illustrated in Fig. 4. In Fig. 4 we show an enlarged range for all samples analyzed. The normalized data sets were normalized by standard methods, taking care to maintain the same energy range, normalization range, and spline range for all samples analyzed. The normalized XANES are illustrated in Fig. 4. In Fig. 4 we show an enlargement of the pre-edge region for these data, including all three newly measured samples plus existing data for BaTiO_3 and EuTiO_3. The region between approximately 4968.5 eV and 4971.5 eV encompasses a peak labeled X, known to correspond to a p admixed final state that arises from hybridization between Ti 3d and O 2p orbitals. This hybridization results from displacement of the Ti atom from the centrosymmetric position within the oxygen octahedron. Vedrinskii et al. have shown that a contribution to the area under peak X is given by Eq. (4) below

$$A = \frac{\gamma_5}{3} d_s^2.$$ (4)

In this equation, $d_s$ is off center Ti displacement and $A$ is a peak area. An experimental determination of the constant $\gamma_5$ by Ravel resulted in values of 11.2 eV/A^2 for BaTiO_3 and 13.6 eV/A^2 for EuTiO_3, with an error bar of about ±3 eV/A^2. It is clear from Fig. 4 that, qualitatively, the Ti displacement is largest for BaTiO_3, smaller and essentially the same for BST, sample A, and sample B, and is significantly less for SrTiO_3 and EuTiO_3. We made use of the results of a recent study by Shuvaeva et al. who utilized the Ba L_3 EXAFS to study the Ti displacement from centrosymmetry in BST, and found that the displacement of Ti in BST is intermediate between that of BaTiO_3 and SrTiO_3. We therefore assume an intermediate $\gamma_5$ of 12.4 eV/A^2 for the BST materials. For EuTiO_3 there is no static Ti displacement, but a small displacement because of thermal vibrations. Unstrained SrTiO_3 is not ferroelectric at any temperature, and we assume the $\gamma_5$ value for SrTiO_3 to be the same as EuTiO_3. These assignments of $\gamma_5$ are rather arbitrary. However the inaccuracies involved do not change the basic conclusion from Fig. 4. This conclusion is that, for the Ta/Y doped BST materials, there is negligible influence of Ta/Y doping or sintering temperature on the average off-center displacement of Ti from the octahedral center of inversion. We measured areas under the spectral peaks between the 4968 eV and 4971 eV energies by a similar method for all samples. Then the peak area of EuTiO_3 in the same energy region was subtracted. The assumption is made that the small peak in EuTiO_3 is entirely due to thermal vibration. Thus, in our procedure, the thermal vibration component is subtracted, so that only the static displacement contribution remains. For calculating the area under spectral peak of EuTiO_3, the experimentally measured values $d_s=0.103$ Å at 300 K and $\gamma_5=13.6±3$ eV/A^2 were used. Figure 5 shows the measured static Ti displacements.

Our measured Ti displacement in undoped BST is intermediate between that of BaTiO_3 and EuTiO_3, in agreement with the recent study by Shuvaeva et al. These results all add credence to the main conclusion of our Ti K-edge study; which is that neither Ta/Y doping into BST nor sintering temperature affects the average Ti displacement, within experimental error. We therefore eliminate differences in average Ti displacement between samples as accounting for the observation that sample A exhibits relaxor behavior and sample B does not.

C. Ta and Y x-ray absorption edge fine structure data

The L_3 extended x-ray absorption edge fine structure (EXAFS) data for the Ta sites in A and B were obtained at beam lines X-11B of the NSLS. Si(111) monochromator crystals were used. The spectra were measured in the fluo-
rescence mode using an ion chamber filled with argon counting gas. Three reproducible spectra were obtained for each sample, aligned, and averaged. For the Ta and Y edges, the data were processed using the Artemis and Athena software packages, and background subtraction was carried out using the AUTOBK code. These programs also enable one to normalize the absorption coefficient $\mu(k)$, and separate the oscillatory EXAFS, $\chi(k)$, from the absorption background. All three data sets were normalized and merged using the same $k$ range $k=2$ to 13 Å$^{-1}$, $k$ weighting of 2 and a hanning $k$ window, for both samples A and B. Figure 6 shows a comparison of the normalized XANES, Fig. 7 shows the corresponding $\chi(k)$ functions (background removed), and Fig. 8 shows the magnitude of the $k^2$ weighted Fourier transform corresponding to the $k$ range 2.5 to 12 Å$^{-1}$ in Fig. 7.

For the Y edges, twenty scans were normalized and averaged. Figure 9 shows the comparison of normalized XANES. Figure 10 shows the corresponding $\chi(k)$ functions.

Figure 11 shows the magnitude of the $k^2$ weighted Fourier transform corresponding to the $k$ range 2 to 15 Å$^{-1}$ range in Fig. 10.

The most striking aspect of the data is that, although there are no obvious differences in the Ta XAFS or FT for samples A and B, the Y XAFS and FT are quite different between these samples. Figure 11 shows that the main Fourier transform (FT) peaks of the EXAFS for sample B (1600 °C sinter) are significantly diminished relative to the FT peaks for sample A (1550 °C sinter). We suspect that some Y atoms have left the perovskite structure in sample B, and that therefore a simple perovskite model for analyzing the XAFS of B is not appropriate.

D. Data analysis

1. Fits for 1550 °C sinter sample

We fit the Ta L$_3$ and Y K-edge data of sample A simultaneously. We considered a model which contains for the third shell a mixture of Ta and Ti for Y centered spectra, and Y and Ti for Ta centered spectra. We imposed the constraint that the number of Ta third shell neighbors to Y equals the number of Y third shell neighbors to Ta. Also, the Debye-Waller term

FIG. 6. Ta L$_3$-edge XANES: background removed and edge step normalized in samples A and B.

FIG. 7. Ta L$_3$-edge EXAFS: Background subtracted and edge step normalized $k^2 \chi k$ in samples A and B.

FIG. 8. Ta L$_3$-edge EXAFS: Fourier transform of $k^2 \chi k$ in samples A and B.

FIG. 5. A plot of the measured static Ti displacements of BaSrTiO$_3$, samples A and B, BaTiO$_3$ and SrTiO$_3$ is given including error bars.
and the distances for Ta-Y and Y-Ta scattering paths were constrained to be the same. We assume a cubic perovskite structure. We have included best fit single scattering paths of first neighbor O and second neighbor Ba and Sr scatterers. We allowed different Debye-Waller terms for each of these paths. Also, we included single scattering (SS), double scattering (DS), and triple scattering (TS) paths for third shell Ti neighbors. For these three classes of paths we chose Debye-Waller factors with constraints (see the Appendix). The number of parameters varied in the fit was less than the number of independent data points. The distance from the central atom for this fit was in the range from 0.8 to 4.4 Å. The $R$ factor for this fit was 0.0283 (Fig. 12). For optimum fit one obtains for the Ta atom that 98% of third shell neighbors are Ti and 2% Y, and for the Y atom that 98% of the third shell atoms are Ti and 2% Ta. However, our error bar for the percentage of clustered atom (Y or Ta) is ±13%. According to the calculations of Crowne, one would expect there to be only small clustering—a 17% chance of a Ta atom around each Y.26 This prediction is barely outside our error bar.

We note that the Ta-O bond lengths obtained from our fits are significantly less than expected based on the average crystal structure and all the Y centered bond lengths, other than Y-Ta, are significantly greater than expectations based on the average crystal structure (Table I). The BST crystallographic lattice constant we obtain from XRD is 3.972 Å, intermediate between the established value of 4.03 Å for BaTiO$_3$ and 3.91 Å for SrTiO$_3$. One might expect, therefore, Ta-O and Y-O bond lengths from EXAFS to be approximately half this intermediate value, or 1.986 Å. In fact, we obtain for our Ta-O and Y-O bond lengths, best fit values of 1.959 Å and 2.181 Å, respectively. The Y-O bond is therefore longer than expected on the basis of the simple model and the Ta-O bond is shorter. Shannon estimates that the ionic radius of Y$^{+3}$ ion in sixfold coordination indeed exceeds the ionic radius of Ta$^{+5}$ ions in sixfold coordination by

**FIG. 9.** Y K-edge XANES: Background subtracted and edge step normalized in samples A and B.

**FIG. 10.** Y K-edge EXAFS: Background subtracted and edge step normalized $k^2\chi k$ in samples A and B.

**FIG. 11.** Y K-edge EXAFS: Fourier transform of $k^2\chi k$ in samples A and B.

**FIG. 12.** This fit result is obtained by fitting Y K-edge and Ta $L_3$-edge EXAFS of sample A simultaneously, and the fit range is $R=0.8$ to 4.4 Å. We show the Fourier transform magnitude of the Y K-edge EXAFS in sample A and fit of theory model which contains for the third shell mixture of Ti and Ta around the Y atom. The insert shows the Fourier transform Ta $L_3$-edge EXAFS in sample A and fit of theory model which contains for the third shell mixture of Ti and Y around the Ta atom.
TABLE I. The best fit values for the nearest neighbor distances are shown. The Y K-edge and Ta L$_3$-edge data of sample A were fit with the model which contains for the third shell a mixture of Ta and Ti around Y atom and Ti and Y around Ta atom. The number(s) in the parentheses correspond to the uncertainty in the last digit(s) of the parameter.

<table>
<thead>
<tr>
<th>Bond</th>
<th>Crystallographic bond length (theory) (Å)</th>
<th>Fit result R (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Y-O</td>
<td>1.986</td>
<td>2.18(1)</td>
</tr>
<tr>
<td>Y-Ba</td>
<td>3.4399</td>
<td>3.54(18)</td>
</tr>
<tr>
<td>Y-Ti</td>
<td>3.9720</td>
<td>4.035(14)</td>
</tr>
<tr>
<td>Y-Sr</td>
<td>3.4399</td>
<td>3.56(22)</td>
</tr>
<tr>
<td>Y-Ta</td>
<td>3.9720</td>
<td>3.96(15)</td>
</tr>
<tr>
<td>Ta-O</td>
<td>1.986</td>
<td>1.959(16)</td>
</tr>
<tr>
<td>Ta-Ba</td>
<td>3.4399</td>
<td>3.392(71)</td>
</tr>
<tr>
<td>Ta-Ti</td>
<td>3.972</td>
<td>4.009(25)</td>
</tr>
<tr>
<td>Ta-Sr</td>
<td>3.4399</td>
<td>3.38(56)</td>
</tr>
<tr>
<td>Ta-Y</td>
<td>3.972</td>
<td>3.96(15)</td>
</tr>
</tbody>
</table>

a factor of 1.4. The ratio of our Y-O to Ta-O distances in this system is actually less drastic than this estimate, and is only 1.1.

2. Fits for 1600 °C sinter sample

We fit the Ta edges of the 1600 °C sinter sample with a model that postulates only Ti in the third shell. An R factor of 0.041 was obtained, which is the best R factor of all our fits. Here the tendency of the Ta centered bond lengths is to be closer to the crystallographically accepted values than for the fit to Ta edges of the 1550 °C sinter sample, but the difference is small and is less than the combined error bars (Table II). We also fit the Y K-edge data of sample B with the above model. The R factor for this fit is 0.0387 and the best fit value for the Debye-Waller factors of Y-Ti scattering paths is 0.0064 (Fig. 13). We note that, whereas the substitutional model for Ta in sample B gives the best R factor (0.0141) the corresponding model for Y in sample B yields the worst R factor of all our fits (0.0387).

We suspect that there may be more than one type of Y site in sample B, and that at the higher temperature sinter, some

TABLE II. The best fit values for the nearest neighbor distances of sample B are shown. These distances are compared to the values for Ta distances of sample A taken from Table I. The number(s) in the parentheses correspond to the uncertainty in the last digit(s) of the parameter.

<table>
<thead>
<tr>
<th>Bond</th>
<th>Crystallographic bond length (theory) (Å)</th>
<th>Fit results (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Sample A</td>
<td>Sample B</td>
</tr>
<tr>
<td>Ta-O</td>
<td>1.986</td>
<td>1.95(16)</td>
</tr>
<tr>
<td>Ta-Ba</td>
<td>3.4399</td>
<td>3.392(71)</td>
</tr>
<tr>
<td>Ta-Ti</td>
<td>3.972</td>
<td>4.009(25)</td>
</tr>
<tr>
<td>Ta-Sr</td>
<td>3.4399</td>
<td>3.38(56)</td>
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</tbody>
</table>

Y has left the perovskite lattice. Yttrium has an extremely high oxygen affinity, as will be discussed below. We have investigated an alternative model which compares the sample B yttrium XAFS, to a superposition of pure Y$_2$O$_3$ XAFS with sample A yttrium XAFS. There are obvious limitations to the validity of this description. For one thing, it is clear from the XRD results that the strain of the 1600 °C sinter sample is significantly less than the strain of the 1550 °C sample, although still large. If it were indeed the case that Y leaves the perovskite lattice to become Y$_2$O$_3$ in sample B, then the remaining perovskite is not really the same material as the perovskite in sample A and therefore this two site Y model is an approximation at best. We found that a combination of about 25% Y$_2$O$_3$ XAFS with 75% sample A Y edge XAFS yielded only a reasonable approximation to the sample B FT in Fig. 11, and we do not believe that we can uniquely determine the nature of the change in the Y environment between samples A and B using XAFS alone. We do note that there are several studies in the literature that find Y components of a system transforming to an oxide upon heat treatment. Choi et al. studied the crystallization of an amorphous YMnO$_3$ layer in a silicon substrate at 870 °C in oxygen. A nanoscale Y$_2$O$_3$ layer formed between the YMnO$_3$ and the silicon substrate, as demonstrated by electron microscopy. The authors point out that the oxidizing ability of Y is about 2.4 times that of manganese, which is itself known as forming a quite stable oxide. Chengzhou et al. have studied Y implants in steel under high temperature oxidation. Y$_2$O$_3$ forms readily due to the great difference between the heats of formation of Y$_2$O$_3$ (−153 kcal/g) versus Fe$_2$O$_3$ (−65.5 kcal/g). We observe no oxide peaks in either sample by XRD; however an informative test of these samples would be to chemically determine the bulk oxygen content of sample B versus A. However, only a truly bulk measurement is acceptable, since if extra oxygen atoms are entering sample B because of the higher temperature sinter, the composition could vary from surface to the bulk. The laboratory of one of us (Potrepka) is purchasing apparatus for combining wet chemical analysis with inductively
coupled plasma mass spectrometry. We intend to analyze our samples by these methods as a part of future studies.

IV. DISCUSSION

We have shed light on the nature of the relaxor sample A. We find no evidence that either the doping with Ta and Y or the different sintering temperatures modify the average Ti displacement from the center of the oxygen octahedron. However, we have shown that an outstanding difference between the relaxor type sample A and the normal ferroelectric B is that the internal stresses in sample A are significantly larger than in sample B. Before summarizing our other findings involving XAFS analysis, we will further discuss results relating to the internal stresses in such materials. Samara demonstrated pressure induced relaxor behavior in various compositionally disordered ferroelectrics.30 Furthermore, Chaabane et al. have found a pressure induced suppression of diffuse scattering in a relaxor ferroelectric.31 Studies by Soon et al. and Ang et al. are particularly germane to the present study. Soon et al. found that A site substitutions of Ba2+ and Sr2+ into Pb0.7La0.3TiO3 generate tensile and compressive internal strains that are associated with relaxor behavior.32 Ang et al. did not study internal strains, but have found that doping Ce into the Ti (B site) of BaTiO3 produces a relaxor material.33

The microstrain in our sample A is large, given the small percentage of Ta and Y dopants. Noheda et al. have determined values of \( \Delta d/d \) for a sample of Pb(Zr0.52Ti0.48) they have manufactured.18 The measured strain value of this sample is \( 2.9 \times 10^{-3} \) or about an order of magnitude less than the difference in the strains between our samples A and B. Balzar et al. have performed a recent theoretical-experimental study of the effect of inhomogeneous strain on the ferroelectric Curie temperature in thin films.34 These samples had a strain of \( 2.5 \times 10^{-3} \). Again, this strain is comparable to the difference in the strains of our samples A and B, which are, furthermore, bulk samples and not subject to the strain from substrate stresses one can obtain in thin films. We note that the strain we determine for B site substitution of both Y3+ and Ta5+ into the 1550 \( ^\circ \)C sample of \( \left[ \text{Ba}_{2x}\text{Sr}_{1-x} \right] \left[ \left( \text{YTa}_{0.05}\text{Ti}_{0.95} \right)\text{O}_3 \right] \) is about half a percent. This strain is slightly greater than the maximum strain of 0.4% obtained by Soon et al. who doped (Ba2+/Sr2+) in the A site to produce (compressive/tensile) strains in Pb0.7(1-x)La0.3TiO3.31 Soon et al. attain a maximum strain for a value of x=0.5 whereas our samples have a larger strain than this at doping levels of Y and Ta of only 3% of the B sites. It is interesting that our sample B with a strain of \( 2.2 \times 10^{-3} \) is a normal ferroelectric, but sample A with a strain only slightly more than twice this value is a relaxor. We note that the c/a ratio of pure ferroelectric BaTiO3 only differs from unity by 1%,15 and speculate that at a threshold value of microstrain, our system may transform from ferroelectric to relaxor.

A conclusion from the XAFS study is that whereas there are no striking differences between the environment of the Ta atoms in sample A versus sample B, there are large differences between the Y edges of these two samples. For the 1550 \( ^\circ \)C sinter sample, the XAFS results can be successfully modeled assuming Ta or Y substitution for Ti in the perovskite lattice; however, the Ta-O bonds are shorter than expected from the crystallography and the Y bonds longer. Our finding of longer Y centered bonds is consistent with the study of Y doped BST thin films by Ven Wang et al., who find an expansion of the unit cell volume after Y doping to Ti sites.35 There are investigations of various substances that imply that such deviations of local bonds from the crystallographically expected length can give rise to a distorted, even buckled structure.36 It is likely that our perovskite structure with Ta or Y inclusions is also distorted.

We consider once again our XRD peak broadening study and the SEM results of Potrepka et al. These results are consistent with grain sizes in the 0.3 micron to 2.0 micron range.2 Arlt et al. have found a correlation between grain size and ferroelectric domain width.38 For BaTiO3, these authors find that for grain sizes of 2 \( \mu \)m, the domain width is roughly 0.3 \( \mu \)m and for grain sizes of 0.5 \( \mu \)m the domain size is approximately 0.1 \( \mu \)m. In the model of Cross for relaxor behavior, the domain size is sufficiently small that the polarization direction of a domain can be changed by thermal energies.12 Different domain sizes will have differing Curie temperatures, which gives a relaxorlike behavior. These domain sizes are estimated by Cross to be of order 100 \( \AA \) or less, which is at least one order of magnitude smaller than the estimate obtained from our XRD or SEM grain size estimates and the results of Arlt et al. On the other hand, Frey and Payne list several studies indicating that the critical size for loss of low temperature tetragonal distortion in pure BaTiO3 may be as large as 0.1 \( \mu \)m.9 However, we do not observe any difference in off center Ti displacement between the larger grained sample B and smaller grained sample A, which may have grain sizes on the order of 0.3 \( \mu \)m or larger. We believe that the grain sizes in our sample A are large enough to cast doubt on the Cross model for the relaxor behavior of this material. Although our XAFS studies show no tendency for clustering of Y and Ta pairs on the nanoscale, the error bars are large enough that the model of Cross cannot be ruled out.12 We do believe that the large internal strains we observe in sample A must be an important component in any explanation of its relaxor behavior.

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APPENDIX: EXAFS DEBYE-WALLER FACTORS OF COLLINAR MULTIPLE-SCATTERING PATHS

For a multiple scattering photoelectron path originating from the absorbing atom, each leg of the path connecting instantaneous atomic positions is given by the vector: \( \mathbf{r}_{i+} = \hat{R}_{i+} + \mathbf{u}_i - \mathbf{u}_i \), where, following the notation of Poikilova and Rehr, \( i+ \) indicates the next nearest neighbor atom to \( i \) in the direction of the path, and \( \hat{R}_{i+} \) and \( \mathbf{u}_i \) correspond to the average leg vector and atomic displacement vector, respectively. EXAFS Debye-Waller factor is defined as:

\[
\sigma_i^2 = \left\langle \left( r_j - R_j \right)^2 \right\rangle = \frac{1}{2} \left\langle \left( \sum_{i=1}^{n_j} \left( \mathbf{u}_i - \mathbf{u}_{i+} \right) \hat{R}_{i+} \right)^2 \right\rangle
\]

where \( \hat{R}_{i+} \) is the unit vector in the direction of \( \mathbf{R}_{i+} \). We now consider collinear paths from the central (absorbing) atom \( a \) to the atom \( c \), where the average positions of atoms \( a, c \), and the intervening atom \( b \) are on the same line. The corresponding DWFs of the single-scattering (SS) \( a-c-a \), double-scattering (DS) \( a-b-c-a \) and the triple-scattering (TS) \( a-b-c-b-a \) collinear paths through intervening atom \( b \) are as follows:

\[
\sigma_{TS}^2 = \sigma_{DS}^2 = \sigma_{SS}^2 = \left\langle \left( \mathbf{u}_a - \mathbf{u}_c \right) \hat{R}_b \right\rangle^2 = \left\langle \mathbf{u}_a^2 \right\rangle + \left\langle \mathbf{u}_c^2 \right\rangle - 2\left\langle \mathbf{u}_a \mathbf{u}_c \right\rangle,
\]

where \( \hat{R}_b \) is the unit vector in the direction of the line connecting average positions of \( a \) and \( c \), and the subscript \( x \) indicates \( x \)-component (along the line containing the atoms) of the displacement vector.

These relationships are modified if the central atom \( (a) \) is between two nearest neighbors \( (b \) and \( c \), all three atoms having their average positions located on the same line. In that case, as in the equation above, the DWF of the SS path \( a-c-a \) is:

\[
\sigma_{SS}^2 = \left\langle \mathbf{u}_a^2 \right\rangle + \left\langle \mathbf{u}_c^2 \right\rangle - 2\left\langle \mathbf{u}_a \mathbf{u}_c \right\rangle.
\]

The DWFs for the DS path \( a-c-b-a \) and TS paths \( a-c-a-b-a \) are equal to each other but not related to the INN SS:

\[
\sigma_{TS}^2 = \sigma_{DS}^2 = \left\langle \mathbf{u}_b^2 \right\rangle + \left\langle \mathbf{u}_c^2 \right\rangle - 2\left\langle \mathbf{u}_b \mathbf{u}_c \right\rangle.
\]

Finally, for the TS path \( a-c-a-c-a \) connecting the central atom and its nearest neighbor \( c \), the DWF is equal to:

\[
\sigma_{TS}^2 = 4\sigma_{SS}^2.
\]

16. S. Heald (private communication).
26. F. Crowne (private communication).