

# Higher Education Math Placement

## Placement Assessment Problem Types

### 1. Whole Numbers, Fractions, and Decimals

#### 1.1 Operations with Whole Numbers

- Addition with carry
- Subtraction with borrowing
- Multiplication with carry
- Introduction to multiplication of large numbers
- Division with carry
- Introduction to exponents
- Order of operations: Problem type 1
- Order of operations: Problem type 2
- Order of operations with whole numbers and exponents: Basic

#### 1.2 Equivalent Fractions and Ordering

- Equivalent fractions
- Simplifying a fraction
- Fractional position on a number line
- Plotting fractions on a number line
- Writing an improper fraction as a mixed number
- Writing a mixed number as an improper fraction
- Ordering fractions with same denominator
- Ordering fractions

#### 1.3 Operations with Fractions

- Addition or subtraction of fractions with the same denominator
- Introduction to addition or subtraction of fractions with different denominators
- Addition or subtraction of fractions with different denominators
- Product of a fraction and a whole number
- Introduction to fraction multiplication
- Fraction multiplication
- Fraction division
- Division involving a whole number and a fraction
- Mixed arithmetic operations with fractions

## 1.4 Decimal Place Value

Rounding decimals

Ordering decimals

## 1.5 Operations with Decimals

Addition of aligned decimals

Decimal addition

Subtraction of aligned decimals

Multiplication of a decimal by a power of ten

Multiplication of a decimal by a whole number

Decimal multiplication: Problem type 1

Division of a decimal by a power of ten

Division of a decimal by a whole number

Converting a fraction to a terminating decimal

## 2. Percents, Proportions, and Geometry

### 2.1 Percentages

Converting between percentages and decimals

Converting a percentage to a fraction

Converting a fraction to a percentage

Writing a ratio as a percentage

Percentage of a whole number

Applying the percent equation

Finding the sale price given the original price and percent discount

Finding the original price given the sale price and percent discount

### 2.2 Proportions

Solving a proportion of the form  $x/a = b/c$

Simple word problem on proportions

Word problem on proportions: Problem type 1

Word problem on proportions: Problem type 2

### 2.3 Perimeter and Area

Perimeter of a square or a rectangle

Finding the missing length in a figure

Finding a side length given the perimeter and side lengths with variables

Area of a square or a rectangle

Area of a piecewise rectangular figure

Area of a triangle

Area of a parallelogram

Finding the side length of a rectangle given its perimeter or area

Circumference and area of a circle

Perimeter involving rectangles and circles

Area involving inscribed figures

## 2.4 Volume and Surface Area

- Volume of a rectangular prism
- Volume of a cylinder
- Surface area of a cube or a rectangular prism
- Surface area of a cylinder

## 2.5 Angles and Triangles

- Solving equations involving vertical angles
- Sum of the angle measures of a triangle)
- Finding an angle measure for a triangle with an extended side

## 2.6 Similar Figures

- Similar polygons
- Indirect measurement

# 3. Signed Numbers, Linear Equations and Inequalities

## 3.1 Integers

- Absolute value of a number
- Integer addition: Problem type 1
- Integer addition: Problem type 2
- Integer subtraction: Problem type 1
- Integer subtraction: Problem type 2
- Integer subtraction: Problem type 3
- Integer multiplication and division

## 3.2 Signed Fractions and Decimals

- Signed fraction addition: Basic
- Signed fraction addition: Advanced
- Signed fraction multiplication: Basic
- Signed fraction multiplication: Advanced
- Signed decimal addition with three numbers

## 3.3 Signed Numbers and Exponents

- Exponents and integers: Problem type 1
- Exponents and signed fractions
- Exponents and order of operations

## 3.4 Algebraic Expressions

- Writing a simple variable expression for a real-world situation
- Evaluating a linear expression in two variables
- Evaluating a quadratic expression in one variable

## 3.5 Properties of Real Numbers

- Distributive property: Whole number coefficients
- Distributive property: Integer coefficients

Combining like terms: Integer coefficients

Combining like terms: Advanced

### 3.6 Solving a Linear Equation with One Occurrence of the Variable

Additive property of equality with decimals

Additive property of equality with integers

Additive property of equality with a negative coefficient

Multiplicative property of equality with whole numbers

Multiplicative property of equality with decimals

Multiplicative property of equality with integers

Multiplicative property of equality with signed fractions

Solving a two-step equation with integers

Solving a two-step equation with signed fractions

### 3.7 Solving a Linear Equation with Several Occurrences of the Variable

Solving a linear equation with several occurrences of the variable: Variables on the same side and distribution

Solving a linear equation with several occurrences of the variable: Variables on both sides and distribution

Solving a linear equation with several occurrences of the variable: Fractional forms with binomial numerators

Solving equations with zero, one, or infinitely many solutions

### 3.8 Applications with Linear Equations

Translating a sentence into a one-step equation

Translating a sentence into a two-step expression

Solving a simple word problem using the formula  $d = rt$

Solving a word problem with two unknowns using a linear equation

Solving a value mixture problem using a linear equation

### 3.9 Solving an Inequality

Graphing a linear inequality on the number line

Graphing a compound linear inequality on the number line

Solving a linear inequality: Problem type 1

Solving a linear inequality: Problem type 2

Solving a linear inequality: Problem type 3

Solving a linear inequality: Problem type 4

Solving a compound linear inequality: Problem type 1

Solving a compound linear inequality: Problem type 2

### 3.10 Solving an Equation or Inequality with Absolute Value

Solving an equation involving absolute value: Basic

Solving an inequality involving absolute value: Basic

### 3.11 Solving a Multivariable Equation for a Variable

Introduction to algebraic symbol manipulation

Algebraic symbol manipulation: Problem type 1

Algebraic symbol manipulation: Problem type 2

## 4. Lines and Systems of Linear Equations

### 4.1 Graphing Lines

Plotting a point in the coordinate plane

Finding a solution to a linear equation in two variables

Graphing a line given its equation in slope-intercept form

Graphing a line given its equation in standard form

Graphing a vertical or horizontal line

### 4.2 Slope of a Line

Finding slope given the graph of a line on a grid

Finding slope given two points on the line

Finding the slope of a line given its equation

Slopes of parallel and perpendicular lines: Problem type 1

### 4.3 Equation of a Line

Finding x- and y-intercepts of a line given the equation: Advanced

Writing the equation of a line given the slope and a point on the line

Writing the equation of the line through two given points

### 4.4 Solving a System of Linear Equations

Graphically solving a system of linear equations

Solving a simple system using substitution

Solving a system of linear equations using elimination with multiplication and addition

Solving a system that is inconsistent or consistent dependent

### 4.5 Graphing Linear Inequalities in the Plane

Graphing a linear inequality in the plane: Standard form

Graphing a linear inequality in the plane: Vertical or horizontal lines

Graphing a system of linear inequalities

### 4.6 Applications with Lines and Systems

Interpreting line graphs

Interpreting the graphs of two functions

Writing an equation and drawing its graph to model a real-world situation

Application problem with a linear function: Problem type 1

Solving a value mixture problem using a system of linear equations

Solving a distance, rate, time problem using a system of linear equations

Solving a percent mixture problem using a system of linear equations

Solving a word problem using a 3 by 3 system of linear equations

## 5. Relations and Functions

### 5.1 Sets and Intervals

Set builder and interval notation  
Union and intersection of finite sets

### 5.2 Evaluating Functions

Evaluating functions: Problem type 1  
Evaluating a piecewise-defined function  
Variable expressions as inputs of functions  
Sum, difference, and product of two functions

### 5.3 Domain and Range

Domain and range from ordered pairs  
Domain and range from the graph of a continuous function  
Domain of a square root function  
Domain of a rational function

### 5.4 Graphs of Functions and their Transformations

Vertical line test  
Finding local maxima and minima of a function given the graph  
Translating the graph of a function: One step  
Transforming the graph of a function by reflecting over an axis  
Transforming the graph of a function by shrinking or stretching  
Writing an equation for a function after a vertical translation  
Writing an equation for a function after a vertical and horizontal translation  
Graphing a simple cubic function  
Graphing a function involving a square root

### 5.5 Composition of Functions and Inverse Functions

Composition of two functions: Basic  
Inverse functions: Problem type 1  
Inverse functions: Problem type 2

## 6. Integer Exponents and Factoring

### 6.1 Properties of Exponents

Writing a positive number without a negative exponent  
Writing a negative number without a negative exponent  
Introduction to the product rule of exponents  
Product rule with positive exponents  
Product rule with negative exponents  
Introduction to the quotient rule of exponents  
Quotients of expressions involving exponents  
Quotient rule with negative exponents: Problem type 1  
Introduction to the power rule of exponents

Power rule with positive exponents

Power rule with negative exponents: Problem type 1

Power rule with negative exponents: Problem type 2

Using the power and product rules to simplify expressions with positive exponents

## 6.2 Scientific Notation

Scientific notation with positive exponent

Scientific notation with negative exponent

## 6.3 Operations with Polynomials

Simplifying a sum or difference of two univariate polynomials

Multiplying a monomial and a polynomial: Univariate with positive leading coefficients

Multiplying a monomial and a polynomial: Multivariate

Multiplying binomials with leading coefficients of 1

Multiplying binomials that are a sum and a difference of two terms: Univariate

Squaring a binomial: Univariate

Multiplication involving binomials and trinomials in two variables

## 6.4 Factoring Polynomials

Greatest common factor of two monomials

Factoring out a monomial from a polynomial: Univariate

Factoring out a monomial from a polynomial: Multivariate

Factoring a quadratic with leading coefficient 1

Factoring a quadratic with leading coefficient greater than 1

Factoring a product of a quadratic trinomial and a monomial

Factoring a difference of squares

Factoring a polynomial by grouping: Problem type 1

# 7. Quadratic and Polynomial Functions

## 7.1 Solving a Quadratic Equation

Solving equations written in factored form

Completing the square

Finding the roots of a quadratic equation with leading coefficient 1

Finding the roots of a quadratic equation with leading coefficient greater than 1

Solving a quadratic equation needing simplification

Applying the quadratic formula: Exact answers

Discriminant of a quadratic equation

Solving a word problem using a quadratic equation with rational roots

Solving a word problem using a quadratic equation with irrational roots

## 7.2 Solving a Quadratic Inequality

Solving a quadratic inequality written in factored form

## 7.3 Graphing a Quadratic Function

Graphing a parabola of the form  $y = ax^2$

Graphing a parabola of the form  $y = (x-a)^2 + c$   
Graphing a parabola of the form  $y = ax^2 + bx + c$ : Integer coefficients  
Rewriting a quadratic function to find the vertex of its graph  
Finding the x-intercept(s) and the vertex of a parabola

## 7.4 Polynomial Functions

Finding zeros of a polynomial function written in factored form  
Finding x- and y-intercepts given a polynomial function  
Determining the end behavior of the graph of a polynomial function  
Inferring properties of a polynomial function from its graph

## 7.5 Circles

Graphing a circle given its equation in standard form  
Graphing a circle given its equation in general form

# 8. Rational Expressions and Functions

## 8.1 Simplifying Rational Expressions

Least common multiple of two monomials  
Simplifying a ratio of polynomials: Problem type 1  
Ratio of multivariate polynomials  
Adding rational expressions with common denominators  
Adding rational expressions with different denominators:  $ax, bx$   
Adding rational expressions with different denominators:  $x+a, x+b$   
Multiplying rational expressions: Problem type 1  
Multiplying rational expressions: Problem type 2  
Dividing rational expressions: Problem type 1  
Complex fractions without variables: Problem type 1  
Complex fraction: Problem type 1  
Complex fraction: Problem type 3

## 8.2 Division of Polynomials

Dividing a polynomial by a monomial: Univariate  
Polynomial long division: Problem type 1

## 8.3 Solving Rational Equations

Solving a rational equation that simplifies to a linear equation: Problem type 1  
Solving a rational equation that simplifies to a linear equation: Problem type 2  
Solving a rational equation that simplifies to a linear equation: Problem type 3  
Solving a rational equation that simplifies to a quadratic equation: Problem type 2

## 8.4 Direct and Inverse Variations

Word problem on direct variation  
Word problem on inverse variation  
Writing an equation that models variation

## 8.5 Graphing Rational Functions

Sketching the graph of a rational function: Constant over linear

Sketching the graph of a rational function: Linear over linear

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## 9. Radicals and Rational Exponents

### 9.1 Simplifying Expressions with Radicals

Square root of a rational perfect square

Square root simplification

Square root of a perfect square monomial

Simplifying a radical expression: Problem type 1

Simplifying a sum of radical expressions

Simplifying a product of radical expressions

Rationalizing the denominator of a radical expression

Rationalizing the denominator of a radical expression using conjugates

### 9.2 Solving Equations with Radicals

Solving a radical equation that simplifies to a linear equation: One radical

Solving a radical equation that simplifies to a linear equation: Two radicals

Solving a radical equation that simplifies to a quadratic equation: One radical

### 9.3 Pythagorean Theorem and the Distance Formula

Pythagorean Theorem

Distance between two points in the plane

### 9.4 Higher Roots

Cube root of an integer

Simplifying a higher radical: Problem type 1

Simplifying a higher radical: Problem type 2

### 9.5 Rational Exponents

Rational exponents: Basic

Rational exponents: Negative exponents and fractional bases

Rational exponents: Powers of powers

Rational exponents: Products and quotients

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## 10. Exponentials and Logarithms

### 10.1 Properties of Logarithms

Converting between logarithmic and exponential equations

Converting between natural logarithmic and exponential equations

Evaluating a logarithmic expression

Basic properties of logarithms

Expanding a logarithmic expression: Problem type 1

Writing expressions as a single logarithm

Change of base for logarithms: Problem type 1

## 10.2 Solving Logarithmic and Exponential Equations

- Solving a logarithmic equation: Problem type 1
- Solving a logarithmic equation: Problem type 2
- Solving a logarithmic equation: Problem type 3
- Solving a logarithmic equation: Problem type 4
- Solving a logarithmic equation: Problem type 5
- Solving an exponential equation: Problem type 1
- Solving an exponential equation: Problem type 2
- Solving an exponential equation: Problem type 3

## 10.3 Graphing Logarithmic and Exponential Functions

- The graph, domain, and range of an exponential function
- The graph, domain, and range of a logarithmic function
- Translating the graph of a logarithmic or exponential function

## 10.4 Applications with Exponential Functions

- Evaluating an exponential function that models a real-world situation
- Solving a word problem using an exponential equation: Problem type 1

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# 11. Trigonometry

## 11.1 Angles

- Converting between degree and radian measure: Problem type 1
- Sketching an angle in standard position
- Reference angles: Problem type 1
- Coterminal angles
- Arc length and central angle measure

## 11.2 Right Triangle Trigonometry

- Sine, cosine, and tangent ratios
- Using a trigonometric ratio to find a side length in a right triangle
- Using a trigonometric ratio to find an angle measure in a right triangle
- Finding trigonometric ratios given a right triangle
- Solving a triangle with the law of sines: Problem type 1
- Solving a triangle with the law of cosines

## 11.3 Unit Circle

- Finding coordinates on the unit circle for special angles
- Trigonometric functions and special angles: Problem type 1
- Trigonometric functions and special angles: Problem type 2
- Finding values of trigonometric functions given information about an angle: Problem type 1
- Finding values of trigonometric functions given information about an angle: Problem type 2

## 11.4 Graphing Trigonometric Functions

Amplitude and period of sine and cosine functions

Amplitude, period, and phase shift of sine and cosine functions

Sketching the graph of a sine or cosine function: Problem type 1

Sketching the graph of a sine or cosine function: Problem type 2

## 11.5 Inverse Trigonometric Functions

Values of inverse trigonometric functions

Composition of a trigonometric function and an inverse trigonometric function: Problem type 2

## 11.6 Trigonometric Identities

Simplifying trigonometric expressions

Sum and difference identities: Problem type 2

Double-angle identities: Problem type 2

## 11.7 Trigonometric Equations

Finding solutions in an interval for a basic equation involving sine or cosine

Finding solutions in an interval for a basic tangent, cotangent, secant, or cosecant equation

Finding solutions in an interval for a trigonometric equation using Pythagorean identities

Solving a basic trigonometric equation involving sine or cosine