

- \_\_\_\_\_ 1. If  $x * y = \frac{1}{2}xy^2$ , then  $3 * 4 =$
- a) 3      b) 6      c) 24      d) 36      e) 72
- \_\_\_\_\_ 2. If  $a \triangleright b = a^2b^3$ , then  $2 \triangleright (-3) =$
- a) -6      b) 72      c) -72      d) 108      e) -108
- \_\_\_\_\_ 3. The operation  $x \star y$  is defined by  $\frac{x-y}{x} + \frac{x-y}{y}$ . What is the value of  $6 \star 4$ ?
- a)  $\frac{1}{6}$       b)  $\frac{1}{5}$       c)  $\frac{2}{5}$       d)  $\frac{1}{2}$       e)  $\frac{5}{6}$
- \_\_\_\_\_ 4. If  $a \natural b = a^2 + b^2$ , then  $(1 \natural 1) \natural 1 =$
- a) 1      b) 2      c) 3      d) 4      e) 5
- \_\_\_\_\_ 5. If  $q \diamond t = q^t - 1$ , then  $2 \diamond (2 \diamond 3) =$
- a) 12      b) 127      c) 181      d) 255      e) 331
- \_\_\_\_\_ 6. If  $a * b = a^2 - b^2$ , what could be a value for  $a$  so that  $a * 2 = 21$ ?
- a) -5      b)  $\sqrt{19}$       c)  $2\sqrt{5}$       d) 25
- e) It cannot be determined from the information given.

- \_\_\_\_\_ 7. If  $x \triangleright y = \frac{1}{2}xy$ , then  $7 \triangleright (4 \triangleright 3) =$   
a) 13      b) 18      c) 21      d) 36      e) 42
- \_\_\_\_\_ 8. If  $\textcircled{x} = \frac{1}{4}x$ , for which of the following values of  $x$  does  $\textcircled{x} = 2$ ?  
a)  $\frac{1}{2}$       b) 2      c) 8      d) 16      e) 32
- \_\_\_\_\_ 9. If  $\boxed{a} = 2a + 1$ , for which of the following values of  $a$  does  $\boxed{a} = \frac{5}{3}$ ?  
a)  $\frac{1}{3}$       b)  $\frac{1}{2}$       c)  $\frac{3}{5}$       d)  $\frac{2}{3}$       e)  $\frac{3}{2}$
- \_\_\_\_\_ 10. If  $\textcircled{x} = (x + 1)^2 - (x - 1)^2 + 1$ , what is the value of  $\textcircled{5}$ ?  
a) 1      b) 10      c) 11      d) 15      e) 21
- \_\_\_\_\_ 11. If the operation  $\heartsuit n$  is defined as  $\heartsuit n = n(n + 1)$ , then  $(\heartsuit 0)(\heartsuit 1)(\heartsuit 2) =$   
a) 0      b) 8      c) 9      d) 12      e) 15
- \_\_\_\_\_ 12. The operation  $\boxed{a}$  is defined as  $a - 2$ . The operation  $\textcircled{a}$  is defined as  $2a$ . Find  $\textcircled{a} - \boxed{a}$ .  
a)  $2a - 2$       b)  $a - 2$       c)  $2a - 4$       d)  $3a - 2$       e)  $a + 2$