

Name: _____

Notes

Date: _____

Converting Forms of a Quadratic Notes

Convert from vertex form to standard form by Multiplying it Out ☺

$$y = (x + 4)^2 - 6$$

Steps:

1. Rewrite the equation as a product of two binomials

$$(x + 4)(x + 4) - 6$$

2. Use FOIL to simplify

$$(x + 4)(x + 4) - 6$$

$$(x^2 + 4x + 4x + 16) - 6$$

3. Combine like terms

$$x^2 + 8x + 10$$

Convert from vertex form to standard form by multiplying the function out.

$$1. f(x) = (x - 1)^2 + 8$$

$$= (x - 1)(x - 1) + 8$$

$$= x^2 - x - x + 1 + 8$$

$$= x^2 - 2x + 9$$

$$2. f(x) = 2(x + 3)^2 - 5$$

$$= 2(x + 3)(x + 3) - 5$$

$$= 2(x^2 + 3x + 3x + 9) - 5$$

$$= 2(x^2 + 6x + 9) - 5$$

$$3. f(x) = -(x - 4)^2 + 3$$

$$= -(x - 4)(x - 4) + 3$$

$$= -(x^2 - 4x + 4x + 16) + 3$$

$$= -(x^2 - 8x + 16) + 3$$

$$= -x^2 + 8x - 16 + 3$$

$$= -x^2 + 8x - 13$$

$$4. f(x) = 2(x + 1)^2 - 2$$

$$= 2(x + 1)(x + 1) - 2$$

$$= 2(x^2 + x + x + 1) - 2$$

$$= 2(x^2 + 2x + 1) - 2$$

$$= 2x^2 + 4x + 2 - 2$$

$$= 2x^2 + 4x$$

Convert from standard form to vertex form by completing the square. BEWARE OF THE A VALUE.

Steps:

$$\begin{aligned}y &= x^2 + 8x + 10 \\y - 10 + \underline{\quad} &= x^2 + 8x + \underline{\quad} \\y - 10 + \underline{16} &= x^2 + 8x + \underline{16} \\y + 6 &= (x + 4)^2 \\y &= (x + 4)^2 - 6\end{aligned}$$

9) $f(x) = x^2 + 8x + 1$

$$\begin{aligned}y - 1 &= x^2 + 8x \\y - 1 + \underline{16} &= x^2 + 8x + \underline{16} \\y + 15 &= (x + 4)^2 \\y &= (x + 4)^2 - 15\end{aligned}$$

10) $f(x) = x^2 + 10x + 20$

$$\begin{aligned}y - 20 &= x^2 + 10x \\y - 20 + \underline{25} &= x^2 + 10x + \underline{25} \\y + 5 &= (x + 5)^2 \\y &= (x + 5)^2 - 5\end{aligned}$$

A VALUES OTHER THAN 1

11) $f(x) = 3x^2 - 6x + 5$

$$\begin{aligned}y - 5 &= 3x^2 - 6x \\y - 5 &= 3(x^2 - 2x + \underline{1}) \\&+ 3(\underline{1})\end{aligned}$$

$$\begin{aligned}y - 3 &= 3(x - 1)^2 \\y &= 3(x - 1)^2 + 3\end{aligned}$$

12) $f(x) = -2x^2 - 16x - 32$

$$\begin{aligned}y + 32 &= -2x^2 - 16x \\y + 32 + \underline{\quad} &= -2(x^2 + 8x + \underline{16}) \\&- 2(\underline{16})\end{aligned}$$

$$\begin{aligned}y + 32 - 32 &= -2(x + 4)^2 \\y &= -2(x + 4)^2\end{aligned}$$