


Absolute Value & Direction of Complex #s

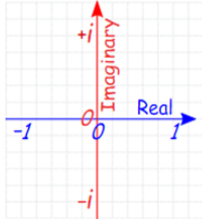
p. 74

Complex Plane



No, **not** that complex plane ...

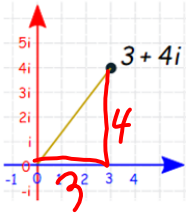
... **this** complex plane:



A plane for **complex** numbers!

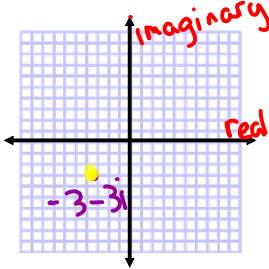
This is a vector.
It has magnitude (length) and direction.

And here is the complex number $3 + 4i$
as a Vector: $(3, 4)$
 $\langle 3, 4 \rangle$

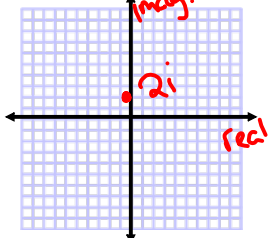


Plot in the complex plane

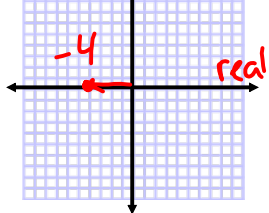
1. $-3 - 3i$
 \nearrow real \uparrow imag.
 like $(-3, -3)$



2. $2i$
 $0 + 2i$
 $(0, 2)$



3. -4
 $-4 + 0i$
 $(-4, 0)$



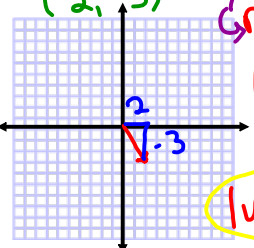
Absolute Value & Direction of Complex #s

Absolute value is the distance from a # to 0 or from the point to the origin, so it is the same as the magnitude of the vector.

1. $2 - 3i$
 $(2, -3)$

Absolute Value
 magnitude
 $|v| = \sqrt{a^2 + b^2}$
 $= \sqrt{(2)^2 + (-3)^2}$
 $|v| = \sqrt{13} \approx 3.6$

direction: $\theta = \tan^{-1}\left(\frac{b}{a}\right)$
 $\theta = \tan^{-1}\left(\frac{-3}{2}\right)$
 $\theta = -56.3^\circ + 360^\circ$
 $\theta = 303.7^\circ$



2. $-2 - 3i$
 $(-2, -3)$ Q III

Abs. Value
 (magnitude):
 $|v| = \sqrt{(-2)^2 + (-3)^2}$
 $|v| = \sqrt{13} \approx 3.6$

Dir: $\theta = \tan^{-1}\left(\frac{-3}{-2}\right)$
 $\theta = 56.3^\circ + 180^\circ$
 $\theta = 236.3^\circ$

