

5-6-19

Aim: SWBAT find the slope of a line given two points on the line.

HW: Packet Pages 21 - 22
Review due Thursday
Test Friday

Do Now: Correct hw, then Quiz

Homework - Slopes and Intercepts of Lines

When an equation is solved for y it is in $y = mx + b$ form

The slope is represented by: m The y-intercept is represented by: b

The coordinates of the y-intercept are: (0, b)

Slopes and Intercepts of Lines: Complete the Chart

The general equation for a line is $ax + by = c$ where a, b and c are any real numbers.

Equation	Equation Solved for y	x-Intercept ($y=0$)	y-Intercept ($x=0$)	Slope
1) $x + y = 5$	$\begin{array}{r} x + y = 5 \\ -x \quad -x \\ \hline y = -x + 5 \end{array}$	$\begin{array}{r} x + y = 5 \\ x + 0 = 5 \\ y = 5 \end{array}$	$\begin{array}{r} x + y = 5 \\ 0 + y = 5 \\ y = 5 \end{array}$	-1
2) $x - y = 4$	$\begin{array}{r} x - y = 4 \\ -x \quad -x \\ \hline -y = -x + 4 \\ y = x - 4 \end{array}$	$\begin{array}{r} x - y = 4 \\ x - 0 = 4 \\ x = 4 \end{array}$	$\begin{array}{r} x - y = 4 \\ 0 - y = 4 \\ -y = 4 \\ y = -4 \end{array}$	1
3) $2x + 5y = 10$	$\begin{array}{r} 2x + 5y = 10 \\ -2x \quad -2x \\ \hline 5y = -2x + 10 \\ y = -\frac{2}{5}x + 2 \end{array}$	$\begin{array}{r} 2x + 5y = 10 \\ 2x + 5 \cdot 0 = 10 \\ 2x = 10 \\ x = 5 \end{array}$	$\begin{array}{r} 2x + 5y = 10 \\ 2 \cdot 0 + 5y = 10 \\ 5y = 10 \\ y = 2 \end{array}$	$-\frac{2}{5}$
4) $3x - 6y = 12$	$\begin{array}{r} 3x - 6y = 12 \\ -3x \quad -3x \\ \hline -6y = -3x + 12 \\ y = \frac{1}{2}x - 2 \end{array}$	$\begin{array}{r} 3x - 6y = 12 \\ 3x - 6 \cdot 0 = 12 \\ 3x = 12 \\ x = 4 \end{array}$	$\begin{array}{r} 3x - 6y = 12 \\ 3 \cdot 0 - 6y = 12 \\ -6y = 12 \\ y = -2 \end{array}$	$\frac{1}{2}$
5) $5x - 2y = 10$	$\begin{array}{r} 5x - 2y = 10 \\ -5x \quad -5x \\ \hline -2y = -5x + 10 \\ y = \frac{5}{2}x - 5 \end{array}$	$\begin{array}{r} 5x - 2y = 10 \\ 5x - 2 \cdot 0 = 10 \\ 5x = 10 \\ x = 2 \end{array}$	$\begin{array}{r} 5x - 2y = 10 \\ 5 \cdot 0 - 2y = 10 \\ -2y = 10 \\ y = -5 \end{array}$	$\frac{5}{2}$
6) $6x + 3y = 12$	$\begin{array}{r} 6x + 3y = 12 \\ -6x \quad -6x \\ \hline 3y = -6x + 12 \\ y = -2x + 4 \end{array}$	$\begin{array}{r} 6x + 3y = 12 \\ 6x + 3 \cdot 0 = 12 \\ 3y = 12 \\ y = 4 \end{array}$	$\begin{array}{r} 6x + 3y = 12 \\ 6 \cdot 0 + 3y = 12 \\ 3y = 12 \\ y = 4 \end{array}$	-2

7) Find the x and y intercept algebraically for $4y + 24x = 16$. **Show work.**

x-intercept (let $y=0$)

$$\begin{aligned} 4y + 24x &= 16 \\ 4(0) + 24x &= 16 \\ \cancel{24}x &= \frac{16}{\cancel{24}} \\ x &= \frac{2}{3} \end{aligned}$$

x-intercept = $\frac{2}{3}$
Coordinates $(\frac{2}{3}, 0)$

y-intercept (let $x=0$)

$$\begin{aligned} 4y + 24x &= 16 \\ 4y + 24(0) &= 16 \\ \cancel{4}y &= \frac{16}{\cancel{4}} \\ y &= 4 \end{aligned}$$

y-intercept = 4
Coordinates (0, 4)

8) Find the x and y intercept algebraically for $2y + 2x = 12$. **Show work.**

x-intercept (let $y=0$)

$$\begin{aligned} 2y + 2x &= 12 \\ 2(0) + 2x &= 12 \\ \cancel{2}x &= \frac{12}{\cancel{2}} \\ x &= 6 \end{aligned}$$

x-intercept = 6
Coordinates (6, 0)

y-intercept (let $x=0$)

$$\begin{aligned} 2y + 2x &= 12 \\ 2y + 2(0) &= 12 \\ \cancel{2}y &= \frac{12}{\cancel{2}} \\ y &= 6 \end{aligned}$$

y-intercept = 6
Coordinates (0, 6)

9) Find the x and y intercept algebraically for $6x - 4y = 36$. **Show work.**

x-intercept (let $y=0$)

$$\begin{aligned} 6x - 4y &= 36 \\ 6x - 4(0) &= 36 \\ 6x &= 36 \\ \cancel{6}x &= \frac{36}{\cancel{6}} \\ x &= 6 \end{aligned}$$

x-intercept = 6
Coordinates (6, 0)

y-intercept (let $x=0$)

$$\begin{aligned} 6x - 4y &= 36 \\ 6(0) - 4y &= 36 \\ -4y &= 36 \\ \cancel{-4}y &= \frac{36}{\cancel{-4}} \\ y &= -9 \end{aligned}$$

y-intercept = -9
Coordinates (0, -9)

Aim: SWBAT find the slope of a line given two points on the line.

Do Now: Given the following equations, name the slope and y-intercept.

$$1) y + 5x = -9$$

$$2) 4y = 12x + 6$$

$$y = -5x - 9 \quad \text{slope} = \underline{-5}$$

$$\text{y-intercept} = \underline{-9}$$

$$y = 3x - \frac{3}{2} \quad \text{slope} = \underline{3}$$

$$\text{y-intercept} = \underline{-\frac{3}{2}}$$

Notes.

To find the actual slope of a line we need to find how the "x" coordinates and the "y" coordinates have changed from point to point. We do this by **finding the difference between the two y-coordinates and the difference between the two x-coordinates.**

Slope is represented by the variable "m".

$$\text{Slope} = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

Since each point has an x-coordinate and a y-coordinate, (x, y), we differentiate between the two by calling them point "1" and point "2".

When you are finding the slope you should BE CONSISTENT!

For Example: Find the slope of a line that contains A (3, 6) and B (2, 7).

(You need to decide which ordered pair you're going to start with first and be consistent with it.)

(Starting with B)

$$m = \frac{\Delta y}{\Delta x} = \frac{7 - 6}{2 - 3}$$

OR

(Starting with A)

$$m = \frac{\Delta y}{\Delta x} = \frac{6 - 7}{3 - 2}$$

$$m = \frac{1}{-1}$$

$$m = -1$$

$$m = \frac{-1}{1}$$

$$m = -1$$

Notice it does not matter which point you start with as long as you are CONSISTENT!

Find the slope of the line that contains each pair of points.

$$1) \quad \overset{x_1}{(3, -9)} \text{ and } \overset{x_2}{(4, -12)}$$

$$2) \quad \overset{x_1}{(1, 0)} \text{ and } \overset{x_2}{(2, 5)}$$

$$\frac{\Delta y}{\Delta x} \rightarrow \frac{y_2 - y_1}{x_2 - x_1} \rightarrow \frac{-12 - (-9)}{4 - 3}$$

$$= \frac{-3}{1} = -3$$

$$\text{slope} = -3$$

$$\frac{\Delta y}{\Delta x} \rightarrow \frac{y_2 - y_1}{x_2 - x_1} \rightarrow \frac{5 - 0}{2 - 1}$$

$$= \frac{5}{1} = 5$$

$$\text{slope} = 5$$

$$3) \quad \begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (0, 3) & \text{and} & (4, 4) \end{matrix}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{4 - 3}{4 - 0}$$

$$m = \frac{1}{4}$$



$$4) \quad \begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (1, -9) & \text{and} & (-3, 1) \end{matrix}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{1 - (-9)}{-3 - 1}$$

$$m = \frac{10}{-4}$$

$$m = \frac{5}{-2}$$

$$5) \quad \begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (6, -1) & \text{and} & (4, -1) \end{matrix}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{-1 - (-1)}{4 - 6}$$

$$m = \frac{0}{-2}$$

$$m = 0$$



$$6) \quad \begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (3, 8) & \text{and} & (3, 1) \end{matrix}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{1 - 8}{3 - 3}$$

$$m = \frac{-7}{0}$$

$$m = \text{undefined}$$



Homework - Finding Slope

Find the slope of the line that contains each pair of points.

1) $\begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (5, 3) & (-1, 1) \end{matrix}$

2) $\begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (-3, 1) & (4, 5) \end{matrix}$

3) $\begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (2, 3) & (-1, 3) \end{matrix}$

4) $\begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (-1, -2) & (2, -5) \end{matrix}$

5) $\begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (5, -2) & (4, -3) \end{matrix}$

6) $\begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (7, 3) & (3, -9) \end{matrix}$

7) $\begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (5, -4) & (5, -9) \end{matrix}$

8) $\begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (1, 0) & (-2, -3) \end{matrix}$

9) Is the equation $y = x^2 - 3$ a linear equation? Answer yes or no. _____

10) Is the equation $y = x + 5$ a linear equation? Answer yes or no. _____

Identify the slope and y-intercept in each equation.

11) $y = -2x + 3$

Slope = _____ y - intercept = _____

12) $y = x - 7$

Slope = _____ y - intercept = _____

Given the slope and y-intercept write an equation in $y = mx + b$ form.

13) $m = -3$ and $b = 4$

14) $m = \frac{1}{4}$ and $b = -5$

Rewrite the following equations in slope-intercept form.

15) $5x - 10y = 25$

16) $5x - y = 8$

Find the x and y intercepts algebraically and write the coordinates of each.

17) $5x - 10y = 25$

18) $5x - y = 8$

19) Graph the equation $y = 5x$, using slope intercept.

Slope = _____

y - intercept = _____

Details of Slope:

