

11-26-18

Aim: SWBAT simplify radical expressions.

HW: Packet Page 13

Quiz Wednesday

Do Now: Correct hw, then top of Page 9

## Homework - Square Roots: Rational or Irrational

- Step 1 - Decide if the number is a "Perfect Square." Answer yes or no.
- Step 2 - State whether the square root is Rational or Irrational.
- Step 3 - If the square root is Irrational then name the two consecutive whole numbers that the non-perfect square root lies between.
- Step 4 - Round the answer to the nearest whole number.

	-Step 1-	-Step 2-	-Step 3-	-Step 4-
	Perfect Square? Yes or No	Rational or Irrational	2 Consecutive Whole Numbers it Lies Between	Rounded answer to the nearest whole number
EX: $\sqrt{8}$	No	Irrational	2 and 3	3
1) $\sqrt{5}$	No	Irrational	2 & 3	2
2) $\sqrt{21}$	No	Irrational	4 & 5	5
3) $\sqrt{35}$	No	Irrational	5 & 6	6
4) $\sqrt{49}$	Yes	Rational		
5) $\sqrt{75}$	No	Irrational	8 & 9	9
6) $\sqrt{89}$	No	Irrational	9 & 10	9
7) $\sqrt{144}$	Yes	Rational		
8) $\sqrt{162}$	No	Irrational	12 & 13	13
9) $\sqrt{196}$	Yes	Rational		
10) $\sqrt{200}$	No	Irrational	14 & 15	14
11) $\sqrt{40}$	No	Irrational	6 & 7	6
12) $\sqrt{400}$	Yes	Rational		

$\sqrt{16}$   $\sqrt{17}$   $\sqrt{25}$

between 4 and 5  
closer to 4

13) Use the number line below to graph the following:  $-\pi$ ,  $-2\frac{4}{8}$ ,  $2.3$ ,  $-\sqrt{16}$ ,  $\sqrt{17}$ ,  $\sqrt[3]{125}$



State whether the following numbers are RATIONAL or IRRATIONAL.

14)  $\pi$  Irrational

15)  $0.\bar{3}$  Rational

16)  $\sqrt{64}$  Rational

17)  $0.242242224\dots$  Irrational

18)  $2.17$  Rational

19)  $\sqrt{21}$  Irrational

20)  $24$  Rational

21)  $-2\frac{1}{3}$  Rational

22)  $\sqrt{100}$  Rational

23)  $\sqrt[3]{8}$  Rational

24)  $-\sqrt{4}$  Rational

25)  $\sqrt[3]{-729}$  Rational

Evaluate.

26)  $\sqrt{225} = 15$

27)  $-\sqrt{64} = -8$

28)  $\pm\sqrt{1} = \pm 1$

29)  $-\sqrt{9} = -3$

30)  $\sqrt[3]{-343} = -7$

31)  $\sqrt[3]{125} = 5$

32)  $\sqrt[3]{64} = 4$

33)  $\sqrt[3]{27} = 3$

When we simplify a fraction, we take out as many common factors as we can.

$$\frac{225}{675} \div \frac{25}{25} = \frac{9}{27} \div \frac{9}{9} = \frac{1}{3}$$

When we simplify a radical (square root) we take out as many perfect squares as we can.

AIM: SWBAT simplify radical expressions.

**DO NOW:**

List the first 15 Perfect Square.

1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225

When is a square root in simplest form?

When its radicand DOES NOT contain any perfect square factors other than 1.

the # inside the  $\sqrt{\quad}$

There are two ways to simplify a radical expression:

**Method 1:** Find the largest perfect square that is a factor of that number.

Example:  $\sqrt{20}$        $\sqrt{20} = \sqrt{4 \cdot 5} = \sqrt{4} \cdot \sqrt{5} = 2\sqrt{5}$        $\sqrt{4} \cdot \sqrt{5}$   
 $\sqrt{20} = 2\sqrt{5}$        $2 \cdot \sqrt{5}$   
 $2\sqrt{5}$

1)  $\sqrt{75}$

$\sqrt{25 \cdot 3}$   
 $\sqrt{25} \cdot \sqrt{3}$   
 $5 \cdot \sqrt{3}$   
 $5\sqrt{3}$

2)  $\sqrt{24}$

$\sqrt{4 \cdot 6}$   
 $\sqrt{4} \cdot \sqrt{6}$   
 $2 \cdot \sqrt{6}$   
 $2\sqrt{6}$

3)  $\sqrt{200}$

$\sqrt{100 \cdot 2}$   
 $\sqrt{100} \cdot \sqrt{2}$   
 $10\sqrt{2}$

4)  $4\sqrt{27}$

$4 \cdot \sqrt{27}$   
 $4 \cdot \sqrt{9 \cdot 3}$   
 $4 \cdot \sqrt{9} \cdot \sqrt{3}$   
 $4 \cdot 3 \cdot \sqrt{3}$

5)  $\sqrt{50}$

$\sqrt{25 \cdot 2}$   
 $\sqrt{25} \cdot \sqrt{2}$   
 $5\sqrt{2}$

6)  $3\sqrt{63}$

$3 \cdot \sqrt{9 \cdot 7}$   
 $3 \cdot \sqrt{9} \cdot \sqrt{7}$   
 $3 \cdot 3 \cdot \sqrt{7}$   
 $9\sqrt{7}$

7)  $\sqrt{50y^2}$

$\sqrt{50} \cdot \sqrt{y^2}$   
 $\sqrt{25 \cdot 2} \cdot y$   
 $\sqrt{25} \cdot \sqrt{2} \cdot y$   
 $5 \cdot \sqrt{2} \cdot y$   
 $5\sqrt{2}y$

8)  $4\sqrt{45}$

$4 \cdot \sqrt{9 \cdot 5}$   
 $4 \cdot \sqrt{9} \cdot \sqrt{5}$   
 $4 \cdot 3 \cdot \sqrt{5}$   
 $12\sqrt{5}$

Method 2: Use its prime factorization to find all the perfect squares.

Example:  $\sqrt{20} = \sqrt{2 \cdot 2 \cdot 5} = \sqrt{2^2 \cdot 5} = 2\sqrt{5}$

9)  $\sqrt{75}$

10)  $\sqrt{24}$

11)  $\sqrt{200}$

12)  $\sqrt{27}$

$$\sqrt{x} = \sqrt{x}$$

$$\sqrt{x^2} = x$$

$$\begin{aligned} \sqrt{x^3} &= \sqrt{x^2 \cdot x} \\ &= \sqrt{x^2} \cdot \sqrt{x} \\ &= x \cdot \sqrt{x} \\ &= x\sqrt{x} \end{aligned}$$

$$\begin{aligned} \sqrt{x^4} &= \sqrt{x^2 \cdot x^2} \\ &= \sqrt{x^2} \cdot \sqrt{x^2} \\ &= x \cdot x \\ &= x^2 \end{aligned}$$

$$\begin{aligned} \sqrt{x^5} &= \sqrt{x^2 \cdot x^2 \cdot x} \\ &= \sqrt{x^2} \cdot \sqrt{x^2} \cdot \sqrt{x} \\ &= x \cdot x \cdot \sqrt{x} \\ &= x^2 \sqrt{x} \end{aligned}$$

$$\begin{aligned} \sqrt{x^6} &= \sqrt{x^2 \cdot x^2 \cdot x^2} \\ &= \sqrt{x^2} \cdot \sqrt{x^2} \cdot \sqrt{x^2} \\ &= x \cdot x \cdot x \\ &= x^3 \end{aligned}$$

$$\sqrt{x^8} = x^4$$

$$\sqrt{x^7} = x^3 \sqrt{x}$$

**Homework - Simplifying Radical Expressions**

List the first 15 perfect squares starting with 1.

\_\_\_\_\_

\_\_\_\_\_

**Simplify each radical expression. Justify your answer.**

1)  $\sqrt{63}$

2)  $\sqrt{99}$

3)  $3\sqrt{99}$

4)  $\sqrt{108}$

5)  $\sqrt{242}$

6)  $\sqrt{128}$

7)  $5\sqrt{18}$

8)  $3\sqrt{8}$

9)  $4\sqrt{200}$

10)  $\frac{2}{3}\sqrt{12}$

11)  $\frac{1}{3}\sqrt{18}$

12)  $\frac{1}{2}\sqrt{20}$