

9-11-17

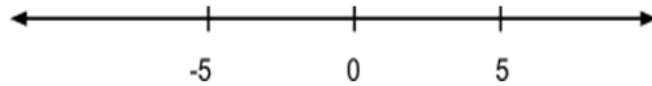
Aim: SWBAT evaluate absolute value and translate expressions
AND define and identify properties of addition and
multiplication.

HW: Packet Pg. 9

Do Now: Packet Pg. 6 # 13 - 18

Notes:

Opposite numbers are the same distance from zero on a number line in opposite directions. For example 5 and -5 are opposites. They are both 5 spaces away from zero.



Zero is a special integer because it is neither positive nor negative.

Why is zero an integer? because it's a whole #

Comparing Integers: > is greater than < is less than

Examples: $36 > 12$ is read "36 is greater than 12"
 $15 < 29$ is read "15 is less than 29"

The number **farther right** on the number line is the **larger** number.

Ex. $15 < 25$ $92 > 63$ $0 < 12$
 $-5 < 0$ $-5 > -18$ $-12 < 12$

Ordering Integers: Order from least to greatest.

$-5, -9, 0, -3$ $-9, -5, -3, 0$ $-2, 7, -5, -1$ $-5, -2, -1, 7$

****The three questions most often missed.**

- *1. Name a number that is not an integer? $\frac{1}{2}$
2. Name the largest negative integer. -1
3. Name the smallest positive integer. 1

Absolute Value measures the _____ a number is from zero on the number line. Distance is always **POSITIVE**, therefore, Absolute Value is ALWAYS _____.

The symbol for absolute value is " $|$ $|$."

$|4|$ "What is the absolute value of 4?" $|4| =$ 4
 $|-4|$ "What is the absolute value of -4?" $|-4| =$ 4

True or False $-4 = 4$ **FALSE** $|-4| = |4|$ **TRUE**
 $4 = 4$

The negative symbol "-" means **opposite**. For example the "opposite of 4" is -4. Simplify the expression. (Start from the inside and work it out)

* 1) $-(-4)$ 4 2) $-(-(-4))$ -4 3) $-[-(-(-4))]$ 4 4) $-(-(-(-(-4))))$ -4

"The opp. of neg. 4"

5) $-|-4|$ -4 6) $-(-|-4|)$ 4 7) $---|-4|$ -4

$5 - 2$ ← subtraction
 -3 ← negative
 "the opposite of 7"
 -7

HOMWORK - SETS OF NUMBERS

****Use the chart we made in class to help you answer these questions!****

Answer the following with...	SOMETIMES	ALWAYS	NEVER
1) Counting Numbers are Whole Numbers.	S	A	N
2) Whole Numbers are Real Numbers.	S	A	N
3) Counting Numbers are Integers.	S	A	N
4) Integers are Counting Numbers.	S	A	N
5) Counting Numbers are Rational..	S	A	N
6) Real Numbers are Irrational.	S	A	N
7) Integers are Rational Numbers.	S	A	N
8) Rational Numbers are Whole Numbers.	S	A	N
9) Whole Numbers are Rational.	S	A	N
10) Rational Numbers are Irrational.	S	A	N

State ALL of the sets of numbers that each of the following belongs to:

	Real	Irrational	Rational	Integer	Whole	Natural
11) 0	R, Rat., I, W					
12) -5	R, Rat, I					
13) 3.421123...	R, Irr					
14) 2.56	R, Rat					
15) 20	R, Rat, I, W, N					
16) $-\frac{3}{5}$	R, Rat.					
17) $0.\bar{6}$	R, Rat.					

Write the OPPOSITE and then ABSOLUTE VALUE of each integer:

18) 7 -7 7

19) -25 25 25

20) 106 -106 106

21) 0 0 0

Complete the Statement with < or >.

22) -6 < 4

23) -2 > -4

24) 0 < 8

Match the integer expression with the verbal expression:

E 25) $-|12|$

A. the opposite of negative twelve

D 26) $|-12|$

B. the absolute value of twelve

C 27) $-|-12|$

C. the opposite of the absolute value of negative twelve

A 28) $-(-12)$

D. the absolute value of negative twelve

B 29) $|12|$

E. the opposite of the absolute value of twelve

Simplify the expression:

30) $-(-9)$
9

31) $|-16|$
16

32) $-|-16|$
-16

The table below shows the distances of the runners from the finish line when the winner won the race. Use the table to answer Questions 33 - 35.

Runner	Distance (ft)
Sarah	-16
Beth	-2
Juanita	0
Tamika	-9
Ingrid	-36

33) Who won the race? Juanita

34) Who finished further back, Sarah or Tamika? Sarah

35) Arrange the girls' names in order from first-place to last-place finish.

(Hint: use a number line to help you)

Juanita Beth Tamika Sarah Ingrid
1st Place 2nd Place 3rd Place 4th Place 5th Place

AIM: SWBAT identify properties of addition and multiplication and use the properties to add integers.

"DO NOW"

Write the opposite of each integer.

- 1) 3 _____ 2) -5 _____ 3) -7 _____ 4) 9 _____

Find the absolute value.

- 5) $|-12|$ _____ 6) $|-4|$ _____ 7) $|9|$ _____ 8) $-|18|$ _____

Compare using < or >.

- 9) 8 _____ -6 10) -7 _____ -4 11) -9 _____ 5 12) -7 _____ -3

Order from least to greatest.

- 13) -1, -6, 0, -3, -5 _____ 14) -18, -20, -15, -17 _____

State ALL the sets of numbers each belongs to.

- 15) -20 _____

- 16) $-\frac{1}{2}$ _____

- 17) $0.\bar{5}$ _____

- 18) π _____

Properties of Addition and Multiplication

- 1) **Commutative Property of addition and multiplication:** (Commutative, \times ; Commutative, $+$)

Changing the order of the numbers without changing the answer. (**#'s commute**)

Examples: A) $2 + 3 = 3 + 2$ B) $4 \cdot 5 = 5 \cdot 4$

- 2) **Associative Property of addition and multiplication:** (Associative, \times ; Associative, $+$)

Moving the **grouping** symbols without changing the answer.

Examples: A) $6 + (2 + 3) = (6 + 2) + 3$ B) $7 \cdot (4 \cdot 6) = (7 \cdot 4) \cdot 6$

- 3) **Additive Identity Property: (Identity, $+$) Identity of # does not change**

Any number plus zero equals that number. **The identity element of addition is zero.*

Examples: A) $9 + 0 = 9$ B) $x + 0 = x$

- 4) **Multiplicative Identity Property: (Identity, \times) Identity of # does not change**

Any number times one is that number. **The identity element of multiplication is one.*

Examples: A) $4 \cdot 1 = 4$ B) $x \cdot 1 = x$

- 5) **Additive Inverse Property: (Inverse, $+$) (Opposites)**

For every number, a , $a + -a = 0$. **Remember: Zero is the identity element*

Examples: A) $9 + -9 = 0$ B) $-x + x = 0$

- 6) **Multiplicative Inverse Property: (Inverse, \times) (Reciprocal)**

For every number, a , $a \cdot \frac{1}{a} = 1$ **Remember: One is the identity element*

Examples: A) $4 \cdot \frac{1}{4} = 1$ B) $x \cdot \frac{1}{x} = 1$

- 7) **Multiplicative Property of Zero: (Zero, \times) (Everything becomes zero)**

Any number times zero is zero

Examples: A) $10 \cdot 0 = 0$ B) $x \cdot 0 = 0$

- 8) **Distributive Property (over addition or subtraction)**

Multiplying a group by a number (term)

Example: A) $4(x + y) = 4x + 4y$ B) $2(3x + 4) = 2 \cdot 3x + 2 \cdot 4$
 $= 6x + 8$

NOTE: You can also use the distributive property backwards by factoring out the GCF

Example: $4x + 14 = 2(2x + 7)$

Name the property for each of the following:

- 1) $(13 + 7) + 8 = 13 + (7 + 8)$ _____
- 2) $0 \cdot (x + 3) = 0$ _____
- 3) $9 \cdot 5 = 5 \cdot 9$ _____
- 4) $(62 + 3) + 0 = (62 + 3)$ _____
- 5) $2(4x + 9) = 8x + 18$ _____
- 6) $(19 + 8) + 6 = (8 + 19) + 6$ _____
- 7) $(2 \cdot 3) \cdot 7 = 2 \cdot (3 \cdot 7)$ _____
- 8) $56 \cdot 1 = 56$ _____
- 9) $2x + 6y = 2(x + 3y)$ _____
- 10) $7 \cdot \frac{1}{7} = 1$ _____
- 11) $-6 + (3 \cdot 8) = -6 + (8 \cdot 3)$ _____
- 12) $-15 + 15 = 0$ _____

Adding Integers

Adding integers means adding with both positive and negative numbers (the whole numbers and their opposites). Before we discuss any rules about adding integers, let's explore . . .

Let's look at some examples together:

- | | | |
|----------------------|----------------------|-----------------------|
| 1) $-2 + 2 =$ _____ | 2) $-4 + 0 =$ _____ | 3) $-5 + 5 =$ _____ |
| 4) $-2 + 5 =$ _____ | 5) $-5 + 2 =$ _____ | 6) $-2 + -5 =$ _____ |
| 7) $-2 + 3 =$ _____ | 8) $2 + -3 =$ _____ | 9) $-2 + -3 =$ _____ |
| 10) $-6 + 1 =$ _____ | 11) $-1 + 6 =$ _____ | 12) $-6 + -1 =$ _____ |

HOMEWORK - Properties & Introduction to Adding Integers

State the name of the property that is shown.

1) $(x + 9) + 1 = x + (9 + 1)$ 1) _____

2) $1 \cdot x = x$ 2) _____

3) $(2 + 3) + 5 = 2 + (3 + 5)$ 3) _____

4) $(12 + 9) + 15 = (9 + 12) + 15$ 4) _____

5) $(2 + 7) \cdot 0 = 0$ 5) _____

6) $12 \cdot (7 \cdot 15) = (12 \cdot 7) \cdot 15$ 6) _____

7) $0 + (9 + 1) = 9 + 1$ 7) _____

8) $3(4x + 9) = 12x + 27$ 8) _____

9) $r \cdot 1 = r$ 9) _____

10) $(8 \cdot 6) \cdot 9 = 8 \cdot (6 \cdot 9)$ 10) _____

11) $106 \cdot 0 = 0$ 11) _____

12) $4(a + b) = 4a + 4b$ 12) _____

13) $-y + y = 0$ 13) _____

14) $(2 + y) + 8 = 8 + (2 + y)$ 14) _____

15) $c \cdot \frac{1}{c} = 1$ 15) _____

16) $(8 \cdot 6) + 9 = (6 \cdot 8) + 9$ 16) _____

17) $-11 + 32 = \underline{\quad}$ 18) $8 + -8 = \underline{\quad}$ 19) $-78 - 15 = \underline{\quad}$ 20) $-25 + 20 = \underline{\quad}$